

Structure II Recitation 3/29

Concrete Beam Design

Guidelines for Final Report

Before we start ...

Today's Tasks:

Homework Example (Concrete Beam Design)

Lab Session (Reinforcement Placement)

Reminder:

Final Report Due Date: 4/12!!!!!!!!!!!!

After tower testing is over and you begin to write the final reports, here are some guidelines to follow.

1. **Clarity of calculations:** Don't just show numbers but give equations and define variables. Make it legible. Either very neatly by hand or use an equation editor like in Microsoft Word. In Word, go to Insert->Object and select Microsoft Equation. In just a few minutes you should be able to get a hang of producing equations. It's pretty simple to use. If you use Excel make sure you label the equations – don't just show results.
2. **Quality of graphics.** You should have clear line-drawings from programs such as Illustrator, AutoCAD, or similar to produce dimensioned drawings of your models. If using Rhino, use the Make2D function to get clear illustrations. Photographs of your final model before and/or after testing will be required in addition to your drawings.
3. **Submit reports on 8-1/2" x 11" paper only.** Reports on 11x17 paper will not be accepted.
4. **Be clean, polished, and professional.** Write clearly, legibly, and with good grammar. Proofread your report before turning it in. Use appropriate professional language in your report. The mark of a good report is one that is easy to understand by someone not familiar with the project.
5. **Turn in the ORIGINAL graded copy of your Preliminary Report with your Final Report.**
6. In the Revised/Tested Tower section of the Final Report (as listed on the Tower Project Tally Sheet - Final Report Requirements), do all the listed calculations for your tower as tested. That is, you should be analyzing the tower that you actually built and tested. This is not a reiteration of the Preliminary Report. We expect that certain changes were made from the preliminary design in your final design.
7. In calculating the overall tower buckling (buckling of whole tower as opposed to individual member buckling), you should use the Moment of Inertia (I) for the tower as a whole. I is taken from the tower cross-section ignoring any cross bracing (only primary vertical members). Using that value for I, you then apply the Euler Buckling Equation, using $K = 1.0$ (this assumes the mass of the load has an inertial force that holds the top in place at the moment of buckling).
8. Mechanical properties for basswood, are given on the preliminary requirements sheet. If you used materials other than basswood, show what values you used for E, F and density. Cite your sources.
9. Throughout your report, check that your numbers are reasonable. If you get, for example, a predicted load capacity of 70 kips, you probably did something wrong.

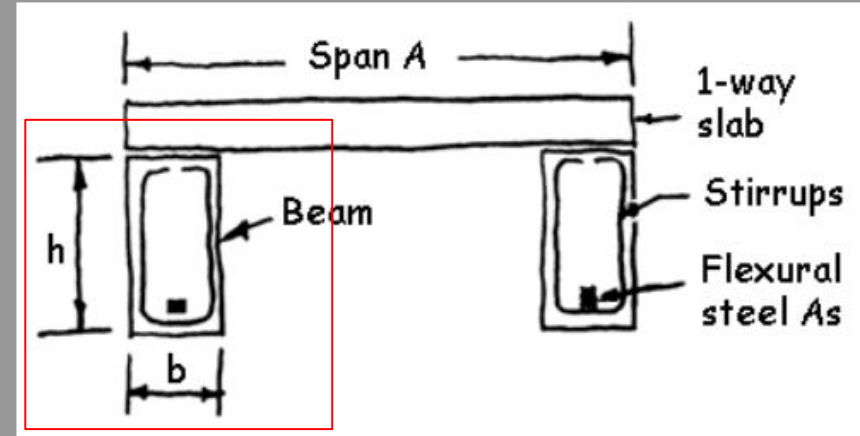
Using the Ultimate Strength Method, analyze the given section to determine its safe moment capacity, M_u , based on the given parameters. Check that the section is tension controlled ($\epsilon_t > 0.005$), and that the amount of steel, A_s is more than the minimum, A_{s_min} .

DATASET: 1

-2-

-3-

Span of slab	18 FT
Span of beam	35 FT
Thickness of slab	11 IN
section width, b	20 IN
section height, h	33 IN
max. aggregate size	0.75 IN
bar size number	7
stirrup bar size number	3
concrete cover	1.5 IN
concrete ultimate strength, f'_c	4500 PSI
steel yield strength, f_y	60000 PSI
Floor Live Load	95 PSF



Designing the steel bar number and actual area

Rectangular Beam Design – Method 1

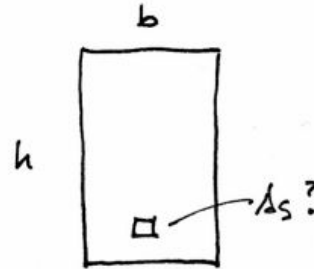
Data:

- Load and Span
- Material properties – f'_c , f_y
- All section dimensions – b and h

Required:

- Steel area - A_s

1. Calculate the factored load and find factored required moment, M_u
2. Find $d = h - \text{cover} - \text{stirrup} - d_b/2$
3. Estimate moment arm $z = jd$, for beams $j \approx 0.9$ for slabs $j \approx 0.95$
4. Estimate A_s based on estimate of jd .
5. Use A_s to find a
6. Use a to find A_s (repeat...until **2%** accuracy)
7. Choose bars for A_s and check A_s max & min
8. Check that $\epsilon_t \geq 0.005$
9. Check $M_u \leq \phi M_n$ (final condition)
10. Design shear reinforcement (stirrups)
11. Check deflection, crack control, rebar development length



$$M_u = \frac{(\gamma_{DL}W_{DL} + \gamma_{LL}W_{LL})l^2}{8}$$

$$A_s = \frac{M_u}{\phi f_y \left(d - \frac{a}{2}\right)}$$

$$a = \frac{A_s f_y}{0.85 f'_c b}$$

$$M_n = A_s f_y \left(d - \frac{a}{2}\right)$$

DL, LL



Required Moment M_u



Required Area A_{req}



Determine Bar Number



Calculate a , β_1 , c , ϵ



Calculate final T, M

Q1: Unfactored Dead Load on Beam from Slab

Volume of the Slab x Density / Beam Span

$(0.5 \times \text{Slab span} \times \text{Beam span}) \times \text{Slab Thickness}$

Density of concrete = 150 pcf

$$(0.5 \times 18 \times 35) \times (11 / 12) \times 150 / 35 = \underline{1237.5 \text{ PLF}}$$

Covert Unit (in to ft)

Q2: Unfactored Dead Load on Beam from Beam (Beam Self Weight)

Volume of the Beam x Density / Beam Span

$(h \times b \times \text{Beam Span})$

$$(33 \times 20 \times 35 / 12^2) \times 150 / 35 = \underline{687.5 \text{ PLF}}$$

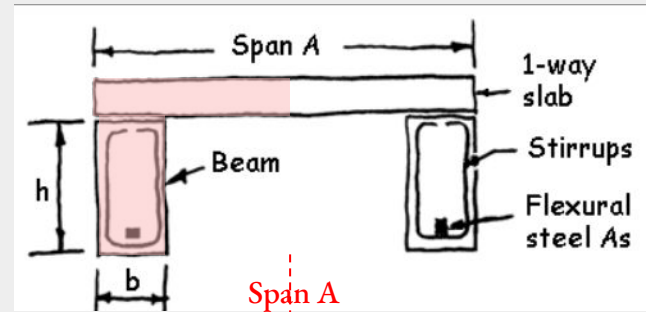
Covert Unit (in to ft)

Q3: Unfactored Live Load on Beam

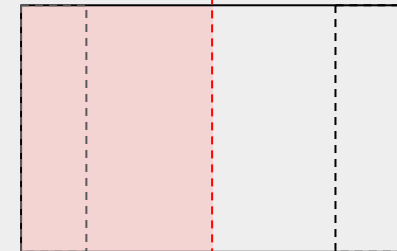
Tributary Area x Floor Live Load / Beam Span

$$95 \times (0.5 \times 18 \times 35) / 35 = \underline{855 \text{ PLF}}$$

DATASET: 1	-2-	-3-
Span of slab		18 FT
Span of beam		35 FT
Thickness of slab		11 IN
section width, b		20 IN
section height, h		33 IN
max. aggregate size		0.75 IN
bar size number		7
stirrup bar size number		3
concrete cover		1.5 IN
concrete ultimate strength, f _c		4500 PSI
steel yield strength, f _y		60000 PSI
Floor Live Load		95 PSF



Top View:



Beam Span

Q4: Total Factored Beam Load (wu)

$$\begin{aligned} w_u &= \underline{1.2 \times (DL (\text{Slab}) + DL (\text{Beam})) + 1.6 \times (LL)} \\ &= 1.2 \times (1237.5 + 687.5) + 1.6 \times (855) \\ &= \underline{3678 \text{ PLF}} \end{aligned}$$

DATASET: 1	-2-	-3-
Span of slab	18 FT	
Span of beam	35 FT	
Thickness of slab	11 IN	
section width, b	20 IN	
section height, h	33 IN	
max. aggregate size	0.75 IN	
bar size number	7	
stirrup bar size number	3	
concrete cover	1.5 IN	
concrete ultimate strength, f _c	4500 PSI	
steel yield strength, f _y	60000 PSI	
Floor Live Load	95 PSF	

Q5: Factored Design Moment from the Loads (Mu)

$$M_u = \underbrace{w_u}_{\text{Q4}} \times L^2 / 8 = (3678 \times 35^2 / 8) / 1000 = \underline{563.19375 \text{ ft-k}}$$

Covert Unit (pounds to kips)

$$1.2W_{DL} + 1.6W_{LL}$$

$$M_u = \frac{(1.2W_{DL} + 1.6W_{LL})l^2}{8}$$

Q6: Distance from Top Beam Edge to Centroid of Flexural Steel (d)

Look at Table A-2 to get the dimensions of the steel bars first,

For my situation:

#7 Flexural Bar, diameter = 0.875 in

#3 Stirrup Bar, diameter = 0.375 in

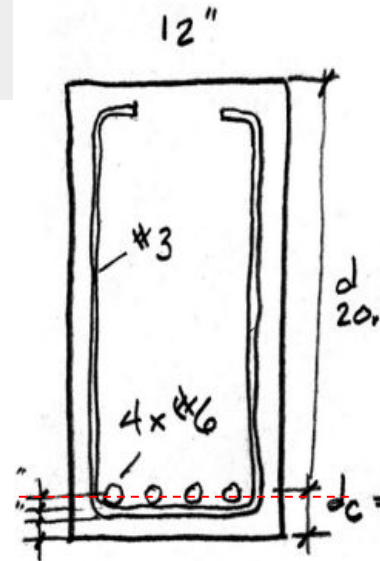
$$d = \text{Section Height} - (\text{Concrete Cover} + \text{Stirrup Bar Diameter} + \text{Flexural Bar Diameter} / 2)$$

$$33 - (1.5 + 0.375 + 0.875 / 2) = 33 - 2.3125 = \underline{\underline{30.6875 \text{ in}}}$$

Span of slab	18 FT
Span of beam	35 FT
Thickness of slab	11 IN
section width, b	20 IN
section height, h	33 IN
max. aggregate size	0.75 IN
bar size number	7
stirrup bar size number	3
concrete cover	1.5 IN
concrete ultimate strength, f _c	4500 PSI
steel yield strength, f _y	60000 PSI
Floor Live Load	95 PSF

Table A.2 Designations, Areas, Perimeters, and Weights of Standard Bars

Bar No.	Customary Units			SI Units		
	Diameter (in.)	Cross-sectional Area (in. ²)	Unit Weight (lb/ft)	Diameter (mm)	Cross-sectional Area (mm ²)	Unit Weight (kg/m)
3	0.375	0.11	0.376	9.52	71	0.560
4	0.500	0.20	0.668	12.70	129	0.994
5	0.625	0.31	1.043	15.88	200	1.552
6	0.750	0.44	1.502	19.05	284	2.235
7	0.875	0.60	2.044	22.22	387	3.042
8	1.000	0.79	2.670	25.40	510	3.973
9	1.128	1.00	3.400	28.65	645	5.060
10	1.270	1.27	4.303	32.26	819	6.404
11	1.410	1.56	5.313	35.81	1006	7.907
14	1.693	2.25	7.650	43.00	1452	11.384
18	2.257	4.00	13.600	57.33	2581	20.238



Q7: The Final Calculated Area of Steel Required (A_s req)

Estimate the moment arm z with $z = 0.95 \times d$ (slab situation)

$$z = 0.95 \times 30.6875 = 29.153$$

$$M_n = \frac{M_u}{\Phi} = A_s \times f_y \times z \quad (\text{Replace } z \text{ with } (d - a/2) \text{ to get } A_s)$$

Q5

Covert Unit (ft-kips to in-pounds)

$$\begin{aligned} A_s &= M_u / (\Phi \times f_y \times z) \\ &= 563.19375 \times 1000 \times 12 / (0.9 \times 60000 \times 29.153) \\ &= 4.293 \text{ in}^2 \end{aligned}$$

Repeat until A_s is within the 2% accuracy

Use A_s to get a :

$$a = A_s \times f_y / (0.85 \times f_c \times b) = 4.293 \times 60000 / (0.85 \times 4500 \times 20) = 3.367 \text{ in}$$

Q6

Use a to get new A_s :

$$\begin{aligned} A_s &= M_u / (\Phi \times f_y \times (d - a/2)) \\ &= 563.19375 \times 1000 \times 12 / (0.9 \times 60000 \times (30.6875 - 3.367/2)) \\ &= 4.315 \text{ in} \end{aligned}$$

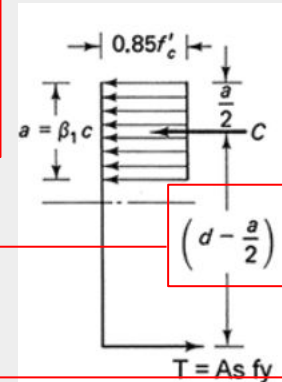
Check if it's within 2% accuracy:

$$(4.315 - 4.293) / 4.293 = 0.005 < 0.02, \text{ It's a pass!}$$

$$A_s \text{ req} = \underline{4.315 \text{ in}^2}$$

3. Estimate moment arm $z = jd$, for beams $j \approx 0.9$ for slabs $j \approx 0.95$
4. Estimate A_s based on estimate of jd .
5. Use A_s to find a
6. Use a to find A_s (repeat...until 2% accuracy)
7. Choose bars for A_s and check A_s max & min

Span of slab	18 FT
Span of beam	35 FT
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Floor Live Load	95 PSF



Moment Arm

$$a = \frac{A_s f_y}{0.85 f'_c b}$$

$$M_n = A_s f_y \left(d - \frac{a}{2} \right)$$

Q8: Number of Rebars Used

Use Table A.2 to find the cross sectional area of the flexural bar,

$$\text{As req} / \text{Cross sectional area of the flexural bar} = 4.315 / 0.6 = 7.1916$$

Round up 7.1916 = 8 rebars

↑
Q7

Q9. Actual, Final Area of Flexural Steel Used (A_s used)

As used

= Cross sectional area of flexural steel x number of rebars

$$= 0.6 \times 8 = \underline{4.8 \text{ in}^2}$$

↑
Q8

Table A.2 Designations, Areas, Perimeters, and Weights of Standard Bars

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14	1.693	2.25	7.650	43.00	1452	11.384
18	2.257	4.00	13.600	57.33	2581	20.238

Q10: Minimum Required Area of Steel ($A_s \min$)

Calculate the two formulas and choose the bigger one:

$$(3 \times (f_c')^{0.5} / f_y) \times b \times d = 3 \times 4500^{0.5} / 60000 \times 20 \times 30.6875 = 2.0586$$

↑
Q6

$$200 / f_y \times b \times d = 200 / 60000 \times 20 \times 30.6875 = 2.0458$$

Since $2.0586 > 2.0458$, $A_s \min = 2.0586 \text{ in}^2$

DATASET: 1	-2-	-3-
Span of slab		18 FT
Span of beam		35 FT
Thickness of slab		11 IN
section width, b		20 IN
section height, h		33 IN
max. aggregate size		0.75 IN
bar size number		7
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concrete cover		1.5 IN
concrete ultimate strength, f_c		4500 PSI
steel yield strength, f_y		60000 PSI
Floor Live Load		95 PSF

$A_s \min$:
greater of (a) and (b)

$$(a) \frac{3\sqrt{f_c'}}{f_y} b_w d$$

$$(b) \frac{200}{f_y} b_w d$$

Q11: Depth of Concrete Stress Block (a)

Q9

$$a = \frac{A_s \times f_y}{(0.85 \times f_c' \times b)}$$

$$= \frac{(4.8 \times 60000)}{(0.85 \times 4500 \times 20)}$$

$$= \underline{\underline{3.7647 \text{ in}}}$$

Q12: Factor Beta 1 (β_1)

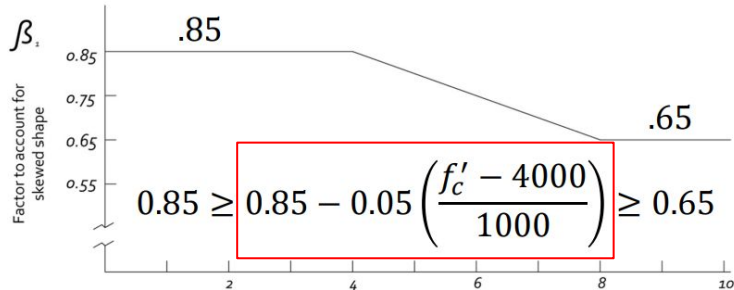
$$\beta_1 = 0.85 - 0.05 \times \left(\frac{f_c' - 4000}{1000} \right)$$

$$= 0.85 - 0.05 \times \left(\frac{4500 - 4000}{1000} \right) = \underline{\underline{0.825}}$$

f_c'	β_1
0	0.85
1000	0.85
2000	0.85
3000	0.85
4000	0.85
5000	0.8
6000	0.75
7000	0.7
8000	0.65
9000	0.65
10000	0.65

Q13: Distance to Neutral Axis from Top of the Beam (c)

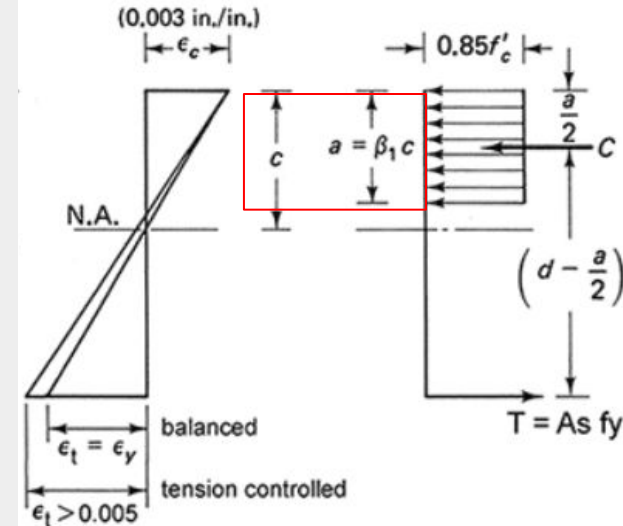
$$c = \frac{a}{\beta_1} = \frac{3.7647}{0.825} = \underline{\underline{4.5633 \text{ in}}}$$



$$a = \frac{A_s f_y}{0.85 f_c' b}$$

$$a = \beta_1 c$$

DATASET: 1	-2-	-3-
Span of slab		18 FT
Span of beam		35 FT
Thickness of slab		11 IN
section width, b		20 IN
section height, h		33 IN
max. aggregate size		0.75 IN
bar size number		7
stirrup bar size number		3
concrete cover		1.5 IN
concrete ultimate strength, f_c'		4500 PSI
steel yield strength, f_y		60000 PSI
Floor Live Load		95 PSF



Q14: Strain in Flexural Steel (ϵ_t)

$$\epsilon_t = (d - c) / c \times (0.003) = (30.6875 - 4.5633) / 4.5633 \times 0.003 = \underline{0.01717}$$

Q6 Q13

Q15: Strength Reduction Factor (Φ)

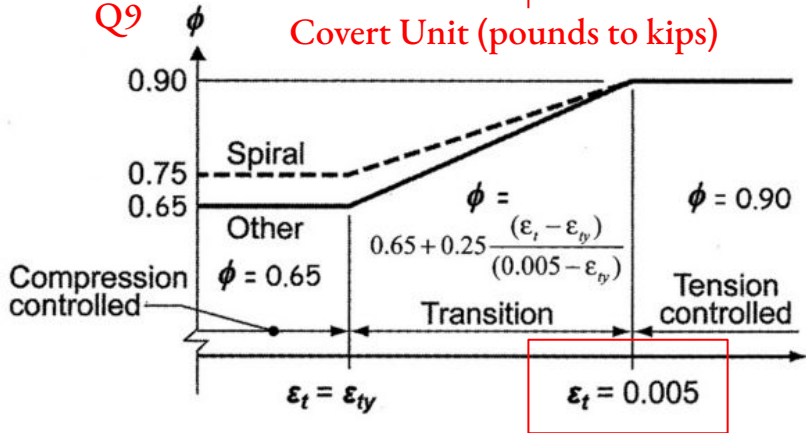
Check if ϵ_t is bigger than 0.005,

Since my ϵ_t is bigger, its tension - controlled, $\Phi = 0.9$

Q16: Tensile Force in the Flexural Steel (T)

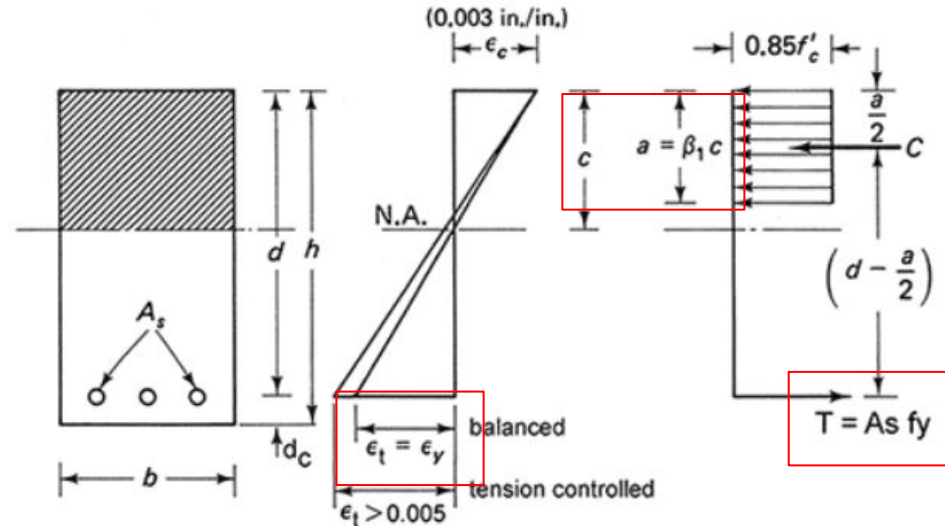
$$T = A_s \times f_y = 4.8 \times 60000 / 1000 = \underline{288 \text{ k}}$$

Q9 Covert Unit (pounds to kips)



PARAMETER	VALUE
Span of slab	18 FT
Span of beam	35 FT
Thickness of slab	11 IN
section width, b	20 IN
section height, h	33 IN
max. aggregate size	0.75 IN
bar size number	7
stirrup bar size number	3
concrete cover	1.5 IN
concrete ultimate strength, f_c	4500 PSI
steel yield strength, f_y	60000 PSI
Floor Live Load	95 PSF

$$\epsilon_t = \frac{d - c}{c} (0.003)$$



Q17: The Nominal Bending Moment (Mn)

$$M_n = T \times (d - (a / 2)) = 288 \times (30.6875 - 3.7647 / 2) = \underline{\underline{8295.88 \text{ k-in}}}$$

Q16 Q6 Q11

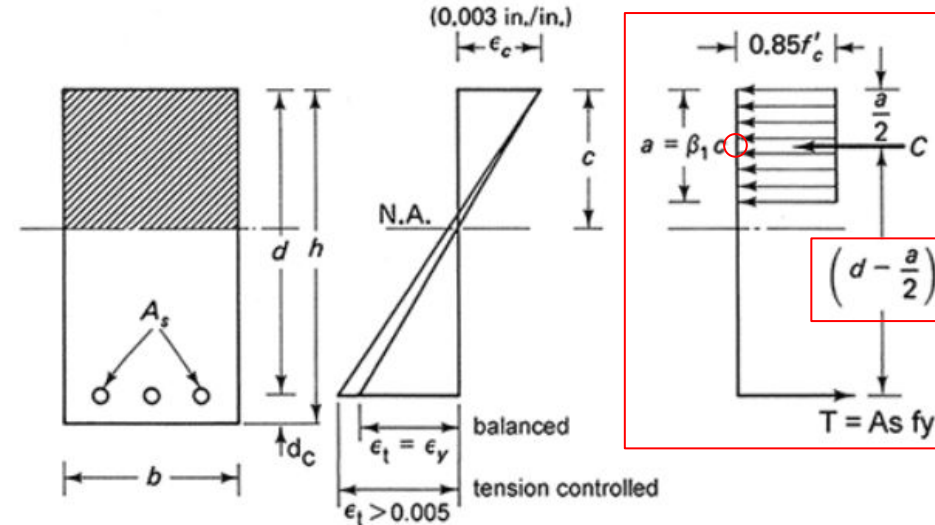
Q18: The Factored Bending Resistance (ΦMn)

$$\Phi M_n = 0.9 \times 8295.88 / 12 = \underline{\underline{622.19 \text{ k-ft}}}$$

Q15 Q17

Covert Unit (in to ft)

$$M_n = T \left(d - \frac{a}{2} \right) = A_s f_y \left(d - \frac{a}{2} \right)$$





Woah, deja vu

Reinforcement Placement

Description

This project produces a graphic representation of the reinforcing layout of a concrete beam.

Goals

- To determine bar diameters and horizontal spacing
- To find the placement and dimensions of a shear stirrup.
- To establish proper cover for reinforcement.
- To draw all beam elements in the proper scale and location.

Procedure

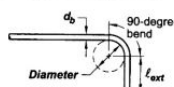
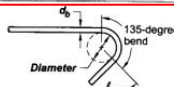
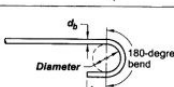
1. For the example beam worked in class, determine the required spacing, s_v and s_h , for the bar size used.
2. For the given stirrup size determine the bend radius for a 90° bend.
3. Make a sketch showing the proper locations of bars and the stirrup including cover.
4. Draw and dimension the depth of the stress block, "a" and the distance to the N.A. from the top of the beam, "c".
5. Dimension and label "d" and "d_c".

Lab Sessions:

Goal:

1. Determine minimum spacings (S_H , S_V)
2. Determine bend radius (90 degree)
3. Calculate d & d_c
4. Calculate a & c
5. Make a sketch of the beam section

Table 25.3.2—Minimum inside bend diameters and standard hook geometry for stirrups, ties, and hoops

Type of standard hook	Bar size	Minimum inside bend diameter, in.	Straight extension ¹⁾ l_{ext} , in.	Type of standard hook
90-degree hook	No. 3 through No. 5	$4d_b$	Greater of $6d_b$ and 3 in.	
	No. 6 through No. 8	$6d_b$	$12d_b$	
135-degree hook	No. 3 through No. 5	$4d_b$	Greater of $6d_b$ and 3 in.	
	No. 6 through No. 8	$6d_b$		
180-degree hook	No. 3 through No. 5	$4d_b$	Greater of $4d_b$ and 2.5 in.	
	No. 6 through No. 8	$6d_b$		

¹⁾A standard hook for stirrups, ties, and hoops includes the specific inside bend diameter and straight extension length. It shall be permitted to use a longer straight extension at the end of a hook. A longer extension shall not be considered to increase the anchorage capacity of the hook.

$f_c' = 3000$ psi

$f_y = 60000$ psi

$d, \text{agg max} = 3/4$ in

Stirrup = #4

Flexural Bar = #9

Steel Bar Number = 4

Concrete Cover = 1.5 in

Section Width = 15 in

Section Height = 36 in

f_c'	β_1
0	0.85
1000	0.85
2000	0.85
3000	0.85
4000	0.85
5000	0.8
6000	0.75
7000	0.7
8000	0.65
9000	0.65
10000	0.65

$$a = \frac{A_s f_y}{0.85 f_c' b}$$

$$c = \frac{a}{\beta_1}$$

Details of Reinforcement

ACI 318 Chapter 25.2
Placement of Reinforcement

- Cover (ACI 20.6.1)
- Horizontal spacing in beams, s_h (ACI 25.2.1)
1 inch
 d_b
 $4/3 d_{\text{agg,max}}$
- Vertical spacing in beams (ACI 25.2.2)
Min 1 inch

Bar size designation	Nominal cross section area, sq. in.	Weight, lb per ft	Nominal diameter, in.
#3	0.11	0.376	0.375
#4	0.20	0.668	0.500
#5	0.31	1.043	0.625
#6	0.44	1.502	0.750
#7	0.60	2.044	0.875
#8	0.79	2.670	1.000
#9	1.00	3.400	1.128
#10	1.27	4.303	1.270
#11	1.56	5.313	1.410
#14	2.25	7.650	1.693
#18	4.00	13.600	2.257

