

Recitation 11

Composite Sections

Homework problem

Composite Sections

10. Composite Sections

Using the strength method, determine the required amount of flexural steel reinforcement, A_s , for the simple span beam (shown in section). The beam carries a dead and live floor load from a one-way slab in addition to its own self weight at 150 PCF. For the given bar size, determine the number of bars to obtain the required A_s . Check $A_{s,min}$ and ϵ_{t} . Calculate the strength moment, M_n for the final beam design and check that ϕM_n is $> M_u$.

DATASET: 1

-2-

-3-

W-section

W16X77

span A

48 FT

span B

13 FT

slab thickness, t

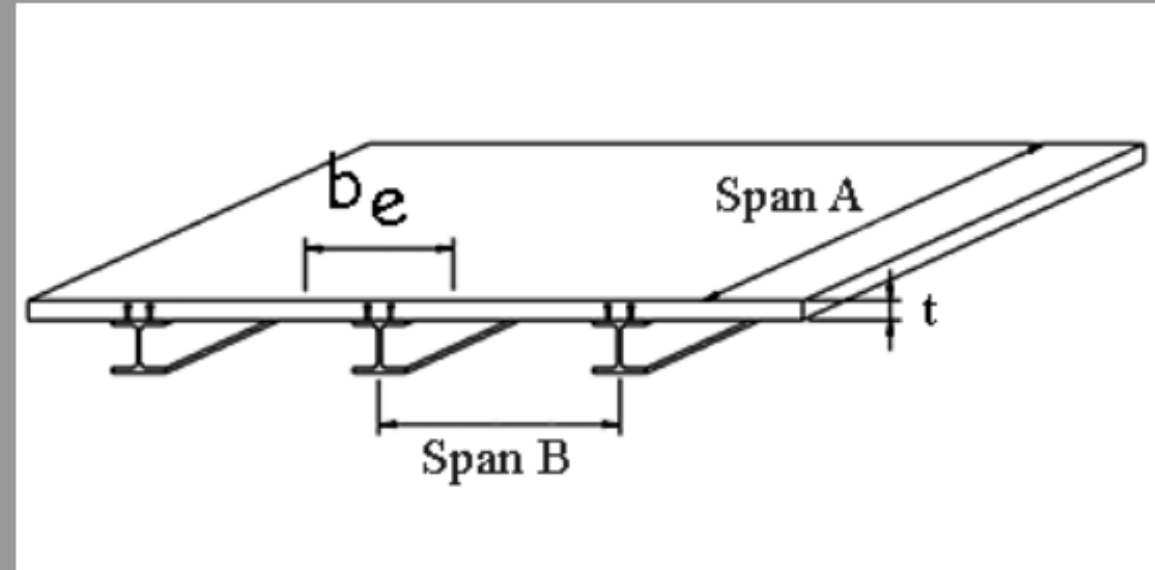
5 IN

steel yield stress, F_y

50 KSI

concrete ultimate stress, f'_c

6 KSI



Q10) Composite sections :-

W-section :- W 16 x 77

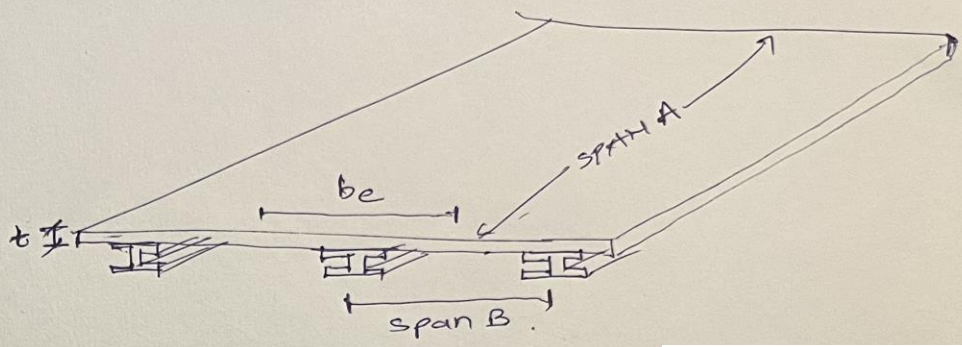
SPAN A :- 48 FT

SPAN B :- 13 FT

Slab thickness, $t = 5$ IN

Steel yield stress, $F_y = 50$ KSI

Concrete ultimate stress, $f'_c = 8$ KSI



1) Effective width of concrete flange, (b_e) :-

b_e is the least total width (overhang + steel flange) of the equations \longrightarrow

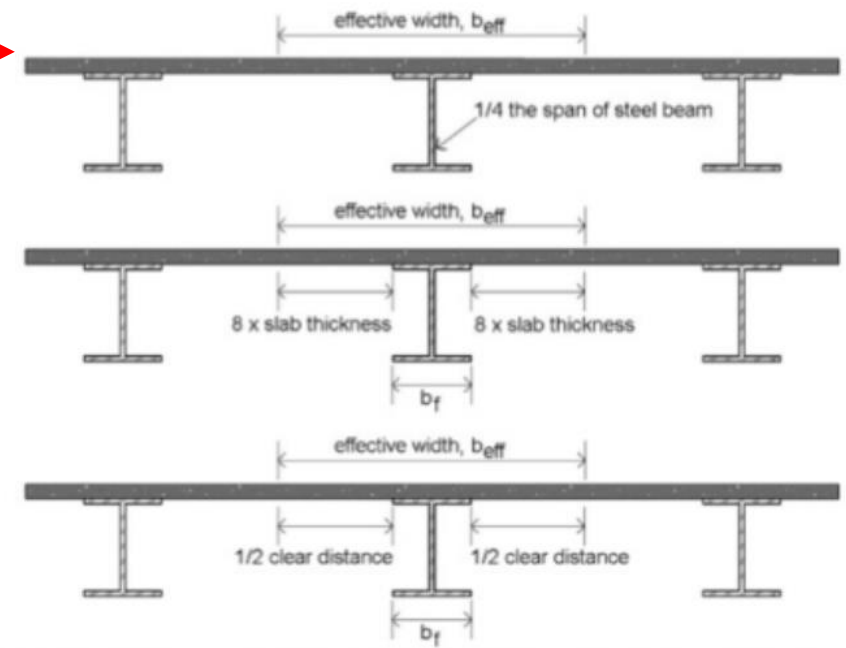
a) Total width = $\frac{1}{4} \times (\text{span A}) \times \frac{12 \text{ in}}{\text{ft}}$
 $= \frac{1}{4} \times 48 \text{ ft} \times \frac{12 \text{ in}}{1 \text{ ft}} = \boxed{144 \text{ in}}$ ←

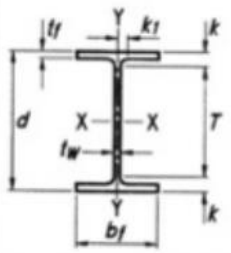
b) Total width = $2 \times 8 \times (t) + (b_f)$ (Table 1-1 AISC table)
 $= 2 \times 8 \times 5 + 10.3 = \boxed{90.3 \text{ in}}$ ← $\text{\textcircled{X}}$ least value governs.

c) Total width = $\text{span B} \times \frac{12 \text{ in}}{1 \text{ ft}}$
 $= 13 \times \frac{12}{1 \text{ ft}} = \boxed{156 \text{ in}}$ ←

b_e is the least total width :

- Total width: $\frac{1}{4}$ of the beam span
- Overhang: 8 x slab thickness
- Overhang: $\frac{1}{2}$ the clear distance to next beam (i.e. b_e is the web on center spacing)

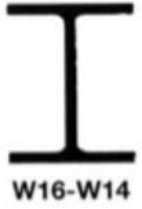




**Table 1-1 (continued)
W-Shapes
Dimensions**

Shape	Area, A in. ²	Depth, d in.	Web		Flange		Distance								
			Thickness, tw in.	tw/2 in.	Width, bf in.	Thickness, tf in.	k		k1 in.	T in.	Workable Gage in.				
							kdes in.	kdet in.							
W16x100	29.4	17.0	17	0.585	9/16	5/16	10.4	10 ³ / ₈	0.985	1	1.39	1 ⁷ / ₈	1 ¹ / ₈	13 ³ / ₄	5 ¹ / ₂
x89	26.2	16.8	16 ³ / ₄	0.525	1/2	1/4	10.4	10 ³ / ₈	0.875	7/8	1.28	1 ³ / ₄	1 ¹ / ₁₆	↓	↓
x77	22.6	16.5	16 ¹ / ₂	0.455	7/16	1/4	10.3	10 ¹ / ₄	0.760	3/4	1.16	1 ⁵ / ₈	1 ¹ / ₁₆	↓	↓
x67 ^c	19.6	16.3	16 ³ / ₈	0.395	3/8	3/16	10.2	10 ¹ / ₄	0.665	1 ¹ / ₁₆	1.07	1 ⁹ / ₁₆	1	↓	↓

**Table 1-1 (continued)
W-Shapes
Properties**



Nominal WT. lb/ft	Compact Section Criteria		Axis X-X				Axis Y-Y				rtb in.	ho in.	Torsional Properties	
	br/2t in.	h/tw in.	I in. ⁴	S in. ³	r in.	Z in. ³	I in. ⁴	S in. ³	r in.	Z in. ³			J in. ⁴	Cw in. ⁶
	100	5.29	24.3	1490	175	7.10	198	186	35.7	2.51	54.9	2.92	16.0	7.73
89	5.92	27.0	1300	155	7.05	175	163	31.4	2.49	48.1	2.88	15.9	5.45	10200
77	6.77	31.2	1110	134	7.00	150	138	26.9	2.47	41.1	2.85	15.7	3.57	8590
67	7.70	35.9	954	117	6.96	130	119	23.2	2.46	35.5	2.82	15.6	2.39	7300

From table 1-1, W 16x77, Area = 22.6 in²
 bf = 10.3 in
 Welft = 77 lb/ft.
 Depth = 16.5 in.
 (d)

Q2) Depth of concrete stress block (a) :-
 from table 1-1, As = 22.6 in²
 from $a = \frac{As f_y}{0.85 f'_c b_e}$ = $\frac{22.6 \text{ in}^2 \times 50 \text{ K/in}^2}{0.85 \times 6 \text{ K/in}^2 \times 10.3 \text{ in}}$
 (slab thickness) = 5 in
 (within slab) → **183** mention (1)

Q4) Nominal bending moment (M_n):-

Q5) The factored bending Resistance, ϕM_n :-

Q6) The factored design moment, M_u :-

from table 1.1 (W16 x 47); $d = 16.5$ in

$$M_n = A_s f_y \left(\frac{d}{2} + t - \frac{a}{2} \right)$$

$$= 22.6 \text{ in}^2 \times 50 \frac{\text{K}}{\text{in}^2} \left(\frac{16.5}{2} + 5 - \frac{2.4537}{2} \right) \text{ in}$$

$$\boxed{M_n = 13,586.1595 \text{ K}\cdot\text{in}} \quad (4)$$

$$\phi M_n = 0.9 \times (13,586.1595) = \boxed{12,227.5436 \text{ K}\cdot\text{in}} \quad (5)$$

$$\therefore M_u = \phi M_n = 12,227.5436 \text{ K}\cdot\text{in} \times \frac{1 \text{ ft}}{12 \text{ in}}$$

$$\boxed{M_u = 1018.96 \text{ K}\cdot\text{ft}} \quad (6)$$

Q7) Total factored design load, M_u :-

$$M_u = \frac{W_u l^2}{8} = \frac{W_u l^2}{8}$$

$$1018.96 \text{ K.ft} = \frac{W_u \times 48^2 \text{ ft}^2}{8}$$

$$\therefore \boxed{W_u = 3.538 \text{ K/ft}}$$

Q8) The self weight of concrete slab :-

$$D_c \text{ slab} = \text{Density} \times \text{slab thickness}$$

$$= 150 \frac{\text{lb}}{\text{ft}^3} \times 5 \text{ in} \times \frac{1 \text{ ft}}{12 \text{ in}}$$

$$= 62.5 \text{ lb/ft}^2$$

Q9) The total (steel + concrete) unfactored dead load on the beam, w_{DL} :-

$$\text{from table 1.1, (W 16 x 77)} \quad w_{DL, \text{steel}} = 77 \text{ lb/ft}$$

$$w_{DL} = w_{DL, \text{concrete slab}} + w_{DL, \text{steel}}$$

$$= D_c \text{ slab} \times L_B + w_{DL, \text{steel}}$$

$$= 62.5 \frac{\text{lb}}{\text{ft}^2} \times 13 \text{ ft} + 77 \text{ lb/ft}$$

$$w_{DL} = 889.5 \frac{\text{lb}}{\text{ft}} \times \frac{1 \text{ k}}{1000 \text{ lb}}$$

$$\therefore w_{DL} = 0.8895 \text{ k/ft}$$

Q10) The actual, unfactored beam live load (capacity), w_{LL} :-

$$W_U^* = 1.2 w_{DL} + 1.6 w_{LL}$$

$$3.538 = 1.2 (0.8895) + 1.6 w_{LL}$$

$$w_{LL} = \frac{3.538 - 1.2 (0.8895)}{1.6}$$

$$w_{LL} = 1.544 \text{ k/ft}$$

Q11) The actual floor live load (floor capacity), LL :-

$$LL = \frac{w_{LL}}{L_B}$$

$$LL = 1.544 \frac{\text{k}}{\text{ft}} \times \frac{1000 \text{ lb}}{1 \text{ k}} \times \frac{1}{13 \text{ ft}}$$

$$\therefore LL = 118.77 \text{ lb/ft}^2$$

Composite Sections

Description

This project allows the students to observe the difference in stiffness between Composite and Non-Composite beam slab combinations.

Goals

- To observe the bending behavior of non-connected beams and slabs
- To observe the bending behavior of a composite section.
- To compare the deflection of the two systems.



Procedure

1. Place the chipboard slab on the foam beam but do not attach the end clips.
2. Place the 10 washer weights in the center and measure the deflection.
3. Repeat the procedure but now with the ends of the slab and the beam clipped together.
4. Again, measure the deflection.
5. Compare the deflections of the two systems.

Due

During recitation

Thankyou !!!